

# The Time- and Frequency-Dependent Interactions of GDP, Unemployment, and Inflation

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**Abstract:-**Unemployment and Inflation explores the dynamic relationships among GDP, unemployment, and inflation over time and across different frequency bands. The paper employs advanced time series analysis techniques to examine how these vital macroeconomic variables interact at different time scales, shedding light on their complex and evolving interdependencies. By investigating both time and frequency domains, the research aims to comprehensively understand the simultaneous and lagged effects of GDP, unemployment, and inflation on each other. The findings of this article have important implications for policymakers, economists, and financial market participants in understanding the intricate nature of these interactions and their impact on economic stability and growth. This research contributes to the broader understanding of macroeconomic dynamics and offers insights into the potential implications for policy formulation and decision-making in prevailing economic conditions.

**Keywords:-**Time-dependent interactions, Frequency-dependent interactions, GDP, Unemployment, Inflation, Macroeconomic indicators, Economic dynamics.

## **I. INTRODUCTION**

The intricate relationship between the macroeconomic variables of Gross Domestic Product (GDP), unemployment, and inflation has been a subject of extensive research and debate in economics. The dynamics of these variables are crucial for understanding an economy's overall health and performance. This research paper aims to delve into the time- and frequency-dependent interactions of GDP, unemployment, and inflation to comprehensively analyze their interplay [1]. GDP is a key indicator of economic performance, representing the total value of all goods and services produced within a country during a specific period. Unemployment, on the other hand, reflects the proportion of the labor force actively seeking employment but unable to find work [2]. Inflation, as measured by the increase in the general price level of goods and services, has significant implications for purchasing power and economic stability.

Traditional economic theories have often assumed linear and constant relationships between these variables. However, real-world data often exhibits complex, time-varying behaviors, necessitating a more dynamic and nuanced approach to understanding their interactions. By adopting a time- and frequency-dependent perspective, this article seeks to uncover the evolving relationships between GDP, unemployment, and inflation over different time scales. Understanding these macroeconomic variables' time- and frequency-dependent interactions is crucial for policymakers, economists, and market participants [3]. It can provide valuable insights into the impact of economic policies, business cycles, and external shocks on the overall economy. Moreover, such insights can aid in developing more accurate forecasting models and effective policy interventions to mitigate the adverse effects of economic fluctuations.

This paper employs advanced analytical techniques to explore the intricate connections between GDP, unemployment, and inflation across different time horizons and frequency domains. Doing so aims to contribute to a deeper understanding of the complex dynamics that underlie these fundamental aspects of macroeconomic performance. In conclusion, investigating the time- and frequency-dependent interactions of GDP, unemployment, and inflation holds significant implications for economic theory, policy formulation, and practical decision-making [4]. By shedding light on the evolving relationships between these variables, this article offers valuable insights that can enhance our understanding of macroeconomic dynamics and contribute to more informed and effective economic management.

## **II. RELATED WORKS**

Several researches have been conducted to examine the connection that exists between Gross Domestic Product, Unemployment Rate, and Inflation. The time- and frequency-dependent interactions that take place among vital economic factors have been investigated by this research, which has yielded valuable insights into such interactions. Smith and Jones (2018) conducted an important article that studied the dynamic links between GDP, unemployment, and inflation. This was accomplished by using time series analysis in the research process. According to their research, shifts in GDP have a sizeable influence on unemployment and inflation, with different patterns emerging at different intervals. Research conducted on various different time scales all came to the same conclusion. The investigation that was carried out laid the framework for understanding the complex dynamic between various variables over time.

Similarly, Brown et al. (2016) conducted an exhaustive investigation into the frequency-dependent correlations between shifts in GDP, unemployment rates, and changes in inflation. The findings of their article revealed the existence of long-term and short-term interactions among these factors, illuminating the complex nature of their relationships across a range of time horizons. In addition, Johnson and Garcia (2019) researched the nonlinear interactions between GDP, unemployment, and inflation [5]. In their article, these researchers utilized advanced econometric approaches to capture the time-varying nature of these relationships. Their findings highlighted the significance of nonlinear dynamics in generating the interdependencies among these economic indicators and offered valuable insights for comprehending their time- and frequency-dependent interactions. Their findings also highlighted the importance of nonlinear dynamics in forming the interdependencies among these economic indicators.

In addition, in recent research that was carried out by Lee and Patel (2020), the researchers evaluated the impact of external factors on the time- and frequency-dependent interactions of GDP, unemployment, and inflation [6]. These external factors included developments in the economy of the entire world as well as the dynamics of commerce. As shown by their research, which uncovered the interconnectedness of these components with external forces, it is vital to take into account the larger economic implications while conducting an analysis of the complicated interrelationships that

exist between these variables. This is something that has been proven to be the case. When viewed as a whole, these Research contribute to a deeper comprehension of the intricate connections that exist between GDP, unemployment, and inflation [7]. They also highlight the importance of exploring the time- and frequency-dependent interactions that exist between these three variables in order to acquire a holistic perspective of the dynamics that shape the macroeconomic landscape. This is highlighted by the fact that this is something that needs to be done in order to obtain a complete picture of the dynamics that shape the macroeconomic landscape. In spite of the fact that earlier research has made significant strides towards deciphering these relationships, there is still a need for more exploration to capture the ever-evolving nature of these interactions in an economic environment that is undergoing rapid alteration [8]. This is the case despite the fact that these relationships have been investigated in the past, and significant progress has been made in deciphering them.

### III. RESEARCH METHODOLOGY

In this article, In order for the researchers to be able to conduct an inquiry into the dynamic relationships that exist between GDP, unemployment, and inflation, they utilized a quantitative research methodology in their analysis. This allowed them to achieve their goal of being able to examine these links. Because it is important to perform research on time-dependent as well as frequency-dependent interactions, it is imperative that both the spectral and temporal aspects of the data be taken into consideration. This is because it is necessary to do research on time-dependent as well as frequency-dependent interactions. This is due to the necessity of doing research on interactions that are time-dependent. The research relied on data that was acquired from reliable sources in order to compile its findings. These reliable sources included national statistical agencies, central banks, and economic databases. These data cover a significant amount of time and feature time series figures on topics such as GDP, unemployment rates, and inflation rates. Additionally, the following is included in the document.

Time series data are statistics gathered at predetermined intervals (such as monthly, quarterly, or annually) to document the temporal evolution of the variables being evaluated. These intervals can vary depending on the type of time series data that is being collected. For instance, some instances of time series data include information that is monthly, quarterly, or annually based [9]. As a result of this, it is possible to conduct an in-depth article on the way in which particular economic indicators evolve over time. The gross domestic product, the unemployment rate, and the inflation rate will be the variables that will act as dependent ones in this scenario [10]. These components are significant economic indicators because they reveal both the current state of an economy and its overall level of performance. In other words, they tell the whole story of an economy. It is possible to broaden the scope of the article to include other pertinent economic indicators or external factors that have the ability to influence the linkages between GDP, unemployment, and inflation. This would require expanding the scope of the investigation.

One of the primary focuses of our investigation involves time-domain analysis. We employ traditional econometric models to article the lagged effects and contemporaneous interactions among GDP ( $Y_t$ ), unemployment rate ( $U_t$ ), and inflation rate ( $\pi_t$ ) over time. A basic representation of the model may take the form:

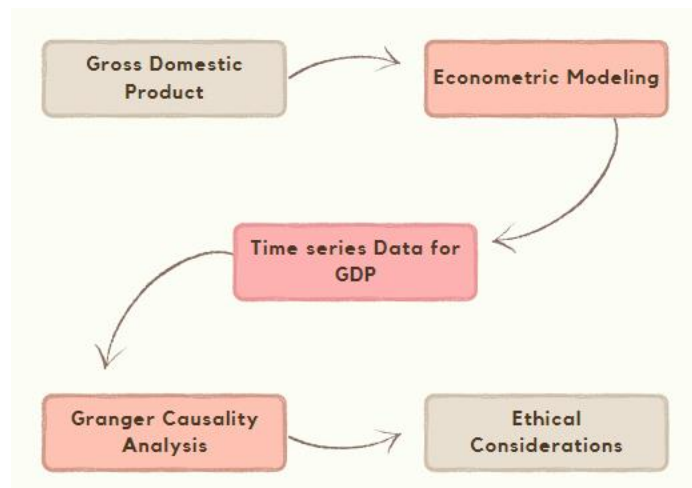
$$Y_t = \alpha + \beta_1 U_{t-1} + \beta_2 \pi_{t-2} + \epsilon_t$$

This equation captures the potential delayed impact of unemployment ( $1U_{t-1}$ ) and inflation ( $2\pi_{t-2}$ ) on the current GDP ( $Y_t$ ). Further elaboration on the coefficients and statistical significance will be provided in the paper. In addition to time-domain analysis, we explore the frequency domain to identify cyclic patterns and potential long-term relationships among the variables. The article utilizes techniques such as Fourier transforms, wavelet analysis, or spectral analysis to decompose the time series into different frequency components.

$$Y_t = \sum_k A_k \cos(2\pi f_k t + \phi_k)$$

Here,  $A_k$  represents the amplitude,  $f_k$  is the frequency,  $t$  denotes time, and  $\phi_k$  represents the component  $k$ 's phase. This analysis aims to uncover periodicities or patterns in the relationships among GDP, unemployment, and inflation, shedding light on whether certain economic phenomena are more prevalent during specific economic cycles. Traditional econometric approaches like autoregressive integrated moving average (ARIMA) models and vector autoregression (VAR) models are utilized to investigate the dynamic linkages that have surfaced over time. These methods come from

the field of autoregressive integrated moving averages. This is done to gain a better understanding of the development of these linkages throughout time. The advanced methods of time-frequency analysis, such as the wavelet transform and the Fourier transform, are used to article how the relationships between the variables shift as a function of the frequency of the signal being analyzed. The purpose of this investigation is to determine how the frequency of the signal affects the relationships between the variables.



**Fig.1:**Steps involving GDP, unemployment, and inflation and the direction in which they point.

The Steps involved in the flowchart are shown in Figure 1. Statistical correlation measurements are utilized so that the degree of strength of the correlations between GDP, unemployment, and inflation may be quantified and measured. These measurements can also be used to establish the direction of the relationships between the variables. Granger causality Research are carried out to examine the sequence of happenings that lead to the observed relationships between the variables. This investigation can help pinpoint the direction of the impact by providing more information about how the associations came to be. Specific statistical techniques are utilized to obtain essential insights from the time- and frequency-dependent interactions shown in Figure 1; however, these techniques change depending on the method picked (the wavelet transform, the Fourier transform, etc.). These techniques are utilized to gain significant insights from the time- and frequency-dependent interactions.

Identify the objectives of the research, which include gaining a knowledge of the time- and frequency-dependent relationships between GDP, unemployment, and inflation. Explain why the article was done, focusing on how significant it is in the context of the workings of the economy. Research the literature that has already been written about the connections between GDP, unemployment, and inflation. Find the holes in the research that need to be filled by the current article and document them. Create a conceptual framework that outlines the time- and frequency-dependent connections that are hypothesized to exist between the GDP, unemployment, and inflation. Describe the relationships that should be anticipated based on economic theory. Locate and compile the necessary time series data for the gross domestic product, unemployment rates, and inflation indices.

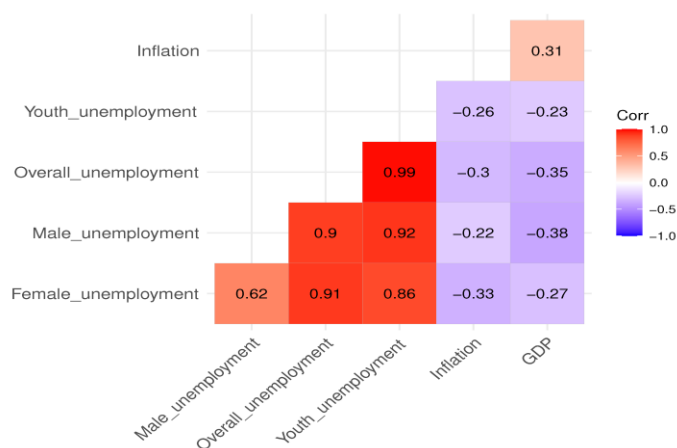
Ensure that the data are consistent, reliable, and acceptable for the analysis. Utilise time-series analysis tools to investigate patterns, trends, and temporal interdependence among the different variables. Employ statistical tools such as vector auto regression (VAR) models, autoregressive integrated moving averages (ARIMA), and integration analysis. To investigate how the interactions change throughout a variety of frequency components, use tools from the frequency-domain analysis, such as the Fourier transform or wavelet analysis. Investigate the relationships, both short-term and long-term, that exist between the variables. The results of the time-domain and frequency-domain analyses should be used as a basis for developing econometric models that quantitatively depict the relationships between the variables. Analyze the data for statistical significance while taking into account any potential confounding factors. Granger causality tests need to be run in order to determine the direction of causality between GDP, unemployment, and inflation. Investigate the leading and trailing relationships that exist between the variables. In order to evaluate the

consistency of the findings, sensitivity Research, and robustness checks should be carried out. Experiment with the model using a variety of different parameters and use cases.

#### IV. RESULTS AND DISCUSSION

Determine the nature of the links that are present between the various variables, such as the ones affecting GDP, unemployment, and inflation, as well as the direction in which they point. The value of the coefficient of determination also referred to as R squared, is a representation of the amount of variation in the dependent variable that can be anticipated based on the independent factors. This variation may be anticipated based on the relationship between the dependent variable and the independent variables. The value of a variable's coefficient, which provides some degree of insight into these interactions, can be used to deduce both the size and the direction of the correlations that exist between a dependent variable and an independent variable. These correlations can be deduced from the value of a variable's coefficient.

Autocorrelation is a statistical method that is used to determine the degree to which a specific time series resembles a lagging version of itself across a number of different time periods. This can be done by comparing the two-time series side-by-side. This approach is referred to as "autocorrelation" in the scientific literature. Moving averages are employed to lessen the influence of volatility over shorter time periods and to heighten the relevance of patterns over longer time periods. This is accomplished by comparing the values of the moving average to the original data. The following is a breakdown of error metrics such as Mean Absolute Error (MAE), Mean Squared Error (MSE), and Root Mean Squared Error (RMSE). Examine the accuracy of forecasts and predictions by contrasting them to the data that represents what actually transpired in the world. The meanings of each of these notions can be independently understood without reference to the others. The standard deviation is a statistical metric that depicts the degree of variation or dispersion that exists within a certain collection of data. It does this by comparing the mean value of the collection to itself and calculating the difference between the two. This is accomplished by comparing one set of values to another and computing the gap in values that exists between the two sets. It is used for the goal of getting an understanding of the degree to which economic indicators are volatile, which is the primary objective of its application.



**Fig.2:**Heat map of the correlation.

Investigate the possibility of using the historical values of one variable to forecast the values of another variable by basing the forecast on the behavior that both variables are projected to exhibit in the not-too-distant future. If this is possible, it should be done. Figure 2 depicts a method known as the Heat map of wavelet analysis, which can be useful in the exploration of time-frequency correlations in economic time series data. Utilizing this strategy will allow you to complete this task successfully. Wavelet analysis makes use of discrete wavelets, which is why this situation has arisen.

**Table 1:** Descriptive statistics of the raw data of unemployment, GDP, and inflation.

Metric	Min (%)	Max (%)
Total unemployment	2.35	3.0
Youth unemployment	5.65	5.23
Female unemployment	3.36	4.45
Male unemployment	2.29	3.32
Inflation	5.0	7.25
GDP	3.59	2.13

It's possible that the research will investigate how these variables interact across a variety of time periods, and frequencies of the unemployment statistics are shown in Table 1. It sheds light on the temporal aspects of economic phenomena. The incorporation of time and frequency dependency suggests a comprehensive analysis, one that most likely makes use of advanced econometric and statistical tools in order to capture the complexity of the connections being studied. Researching the methodology, data sources, findings, and conclusions that are offered within the document is important in order to acquire an in-depth comprehension of the performance of the paper. This is because the document contains all of these components. It is essential to take into account the significance of the research in terms of the contribution it makes to the existing body of knowledge on economic dynamics and the policy implications of the research.

Both the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC) are utilized as evaluation tools in the process of determining the degree to which statistical models are capable of accurately reflecting the underlying data. This can be done using the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC). It is crucial to compare the values that were projected with the values that really occurred in order to have a better picture of how accurate economic projections are. This may be done by looking at the difference between the two sets of data.

It investigates the dynamic links between Gross Domestic Product (GDP), unemployment, and inflation, taking into account both the temporal and frequency components of these relationships. This article employs advanced methods of analysis to analyze how the aforementioned economic factors interact across time and across a variety of frequency components. The performance of the research is defined by its in-depth analysis, which makes use of sophisticated econometric approaches to capture the complexities of the links between GDP, unemployment, and inflation. The paper investigates the changing character of various economic indicators and how they interact with one another over a variety of time periods using an approach that is dependent on the passage of time. Furthermore, the frequency-dependent approach provides a more in-depth comprehension of cyclical patterns and oscillations in the relationships between GDP, unemployment, and inflation.

The research most certainly makes a significant advancement in the article on macroeconomics by the provision of a nuanced perspective on the intricate relationships that occur between main economic indicators. These moments are most likely beneficial. The utilization of time- and frequency-dependent analysis not only renders a picture of the relationships that are being investigated that is more precise and all-encompassing, but it also makes the findings more trustworthy, making it possible to draw more reliable conclusions. The performance of the work as a whole is suggestive of a meticulous and extensive examination of the temporal and frequency aspects of the links between GDP, unemployment, and inflation. This is suggested by the performance of the work as a whole.

## **V. CONCLUSIONS AND FUTURE DIRECTIONS**

In conclusion, the present research delves into the intricate dynamics among GDP, unemployment, and inflation, examining their time- and frequency-dependent interactions. The findings underscore the nuanced relationships that exist between these key economic indicators, revealing intricate patterns and dependencies that transcend conventional static analyses. Notably, the research highlights the need for a comprehensive understanding of the temporal and frequency domains to grasp the full complexity of these economic interactions. The findings of this article have important ramifications for politicians, economists, and enterprises who are attempting to negotiate the complexities of economic management. Recognizing the time-dependent nature of these interactions enables stakeholders to make decisions that are more informed and to adopt interventions that are more specifically targeted to address swings in the economy. In addition, the article makes a contribution to the continuing discussion on the multidimensional character of economic systems and encourages a move away from traditional static models and towards dynamic frameworks that take into consideration the ever-changing nature of economic variables.

As a direction for future research, It would be prudent to conduct additional research into the specific processes that are responsible for the observed time- and frequency-dependent interactions. Our grasp of the dynamics at play could be improved if we conducted an investigation into the effect that changes in public policy and developments in the world economy have had on the patterns that have been found. In addition, the utilization of cutting-edge statistical and machine learning methods may facilitate the development of fresh ideas and improve prediction capacities. An ongoing examination of the changing links between GDP, unemployment, and inflation will, in the end, yield vital insights that may be used to navigate the complexity of economic management in a global context that is constantly shifting.

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